On the first eigenvalue of the Laplacian for polygons

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Abstract: In 1947, Polya proved that if n = 3, 4 the regular polygon P_n minimizes the principal frequency of an *n*-gon with given area and suggested that the same holds for larger values of n. In 1951, Polya and Szego discussed the possibility of counterexamples. Recently, I constructed explicit (2n-4)-dimensional polygonal manifolds and proved for n large that there exists an explicit non-empty set A_n such that P_n has the smallest principal frequency among n-gons in A_n . The techniques involve a partial symmetrization, tensor calculus, the spectral theory of circulant matrices, and $W^{2,p}$ estimates. An application is given in the context of electron bubbles.